



Rare B Decays

Adrian Bevan*

KEK Topical Conference 6
(Feb 6th-8th 2007)

~~Note: L. Silvestrini is giving a theory talk on this subject on Thursday.~~

*From the BaBar Collaboration

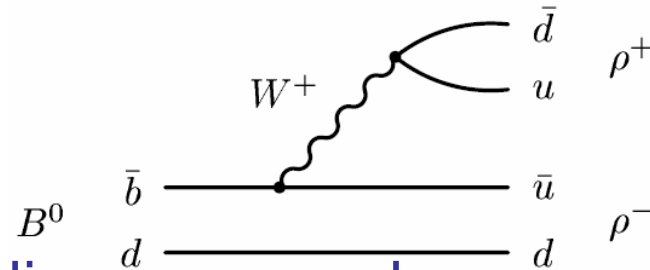
Overview

- General Motivation
- The KEK-B/PEP-II and the Belle/BaBar detectors
- Results
 - (Semi-)Leptonic and radiative rare B decays
 - $B \rightarrow l\nu$,
 - $B \rightarrow K^*ll$
 - $B \rightarrow d\gamma$ transitions
 - Hadronic charmless rare B decays
 - $K^*\rho$
 - $a_1\rho$
 - $\rho\pi$
 - Searches for direct CP violation
- Summary

General Motivation

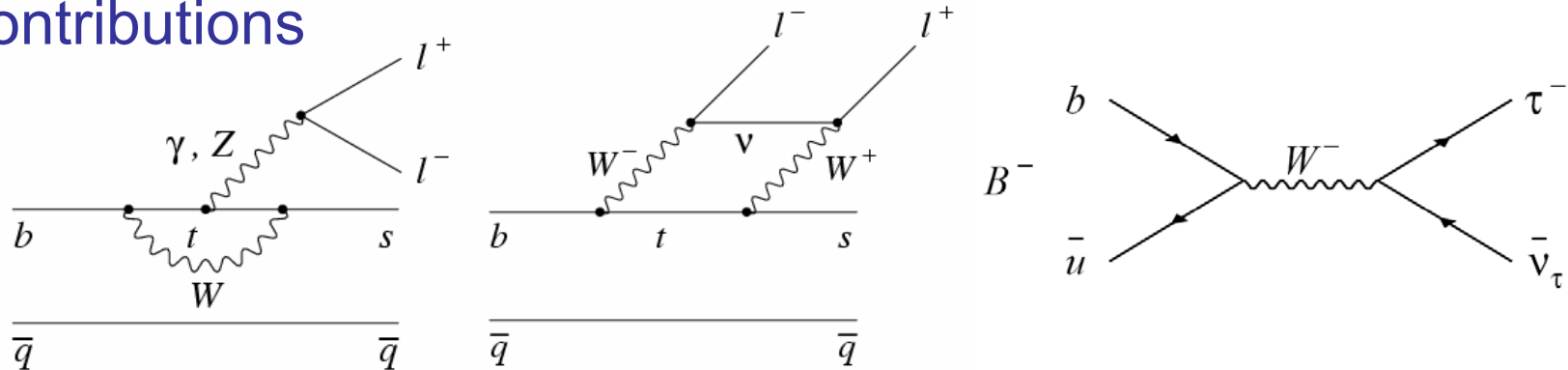
- Tree level contributions are understood well

Large Branching Fractions



- Higher order diagrams can be more difficult to calculate, and can be sensitive to new heavy particles (H^+ , SUSY particles etc.). Many rare decays only have higher order contributions

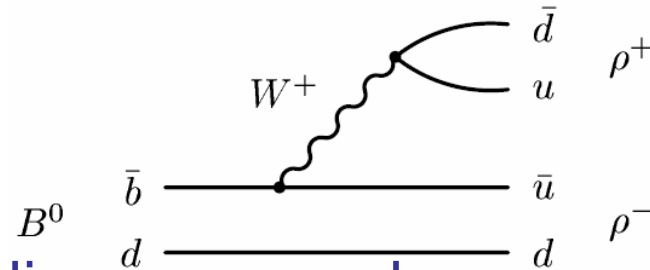
Small Branching Fractions (Rare)



General Motivation

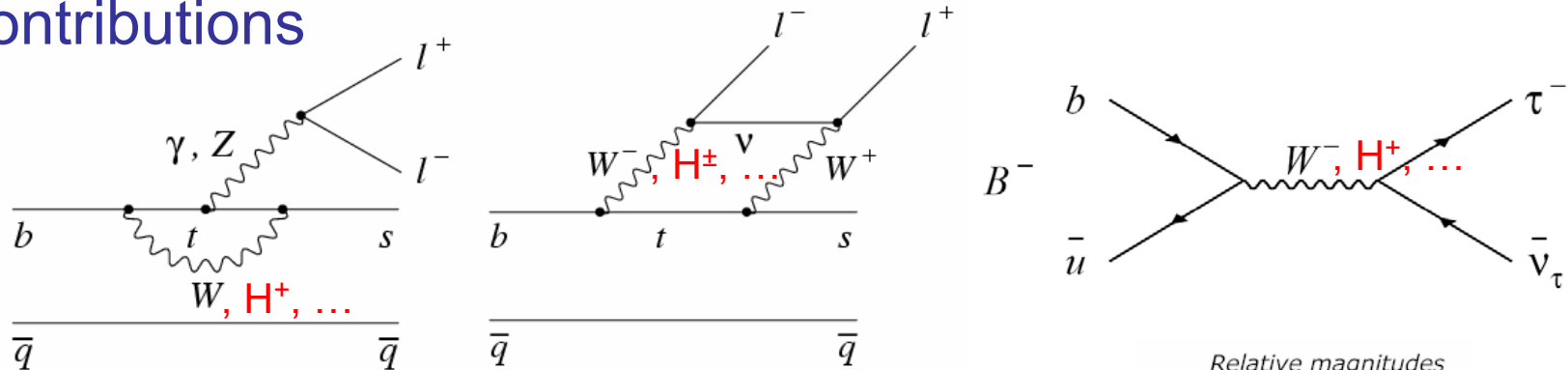
Large Branching Fractions

- Tree level contributions are understood well



- Higher order diagrams can be more difficult to calculate, and can be sensitive to new heavy particles (H^+ , SUSY particles etc.). Many rare decays only have higher order contributions

Small Branching Fractions (Rare)



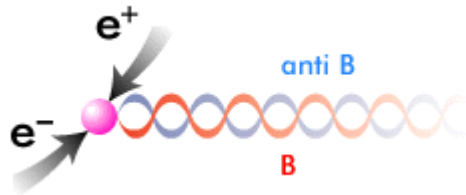
- Provide useful tests of loop calculations.
- Could help us look beyond the SM.
- CKM matrix helps us estimate hierarchy of related decays.

Relative magnitudes

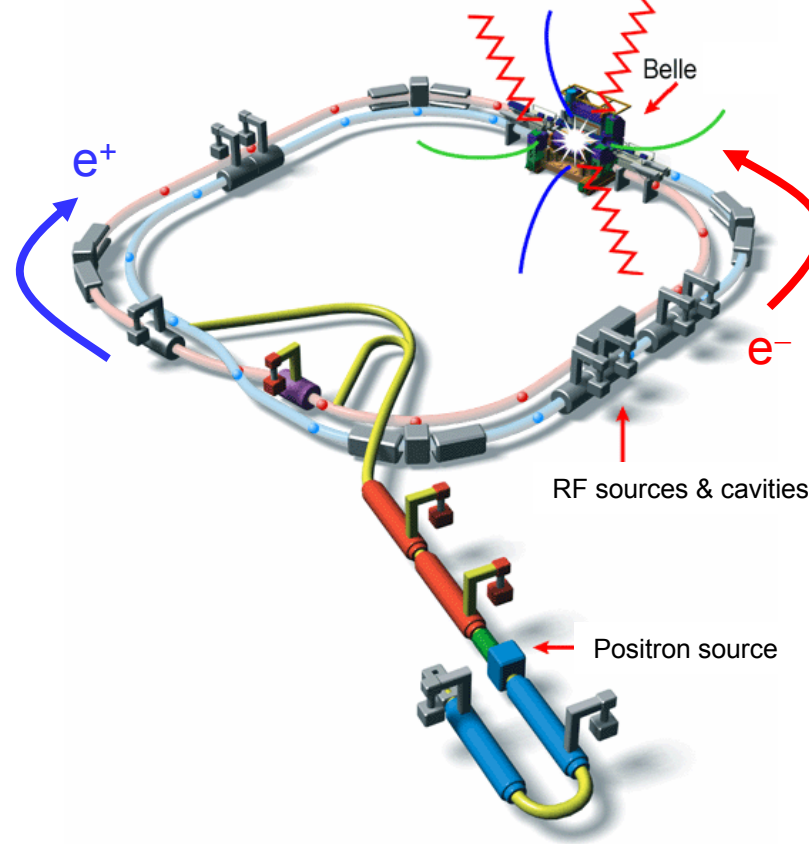
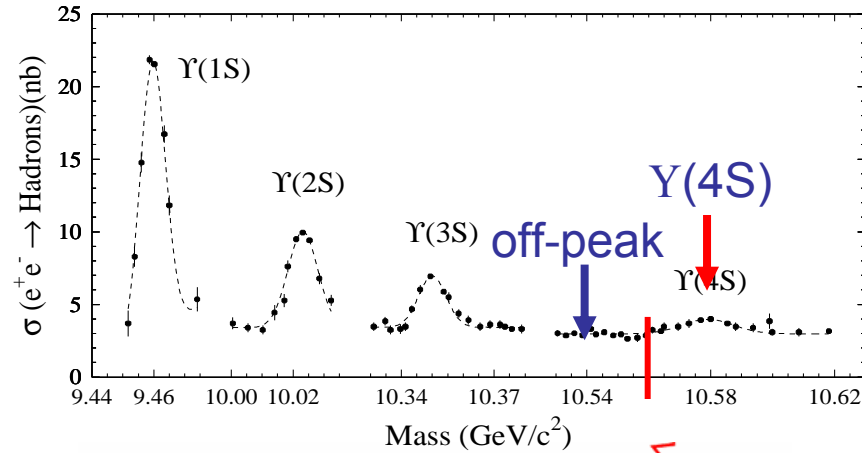
$$V_{CKM} = \begin{matrix} & \begin{matrix} d & s & b \end{matrix} \\ \begin{matrix} u \\ c \\ t \end{matrix} & \begin{pmatrix} \blacksquare & \blacksquare & \cdot \\ \blacksquare & \blacksquare & \blacksquare \\ \cdot & \blacksquare & \blacksquare \end{pmatrix} \end{matrix} \quad 4$$

KEK-B/PEP-II

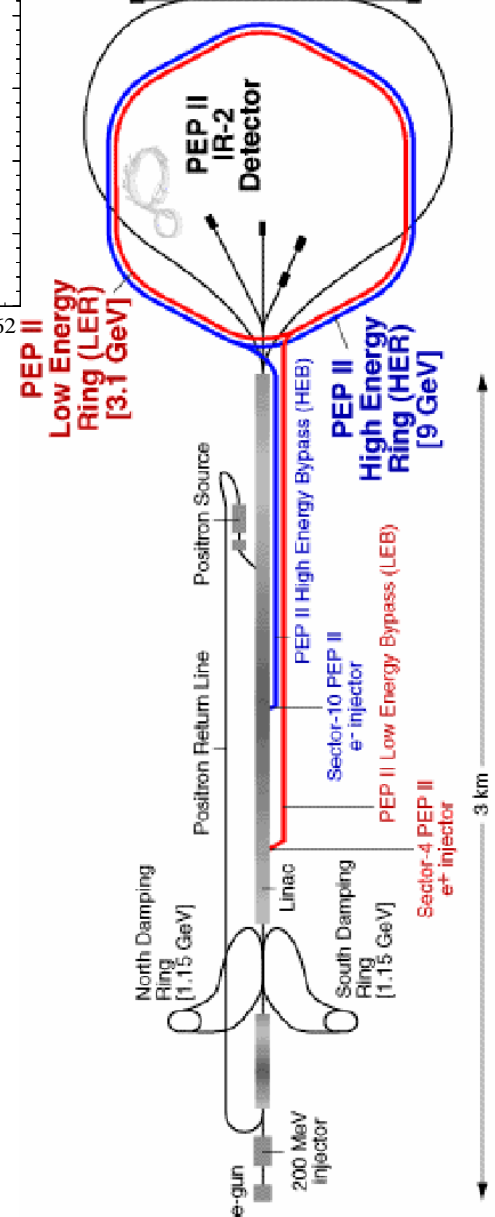
- Asymmetric energy e^+e^- collider
- Study decay of B meson pairs.



- Record data at the $Y(4S) \sim 90\%$ of the time.
- Run below the $b\bar{b}$ production threshold for background studies.



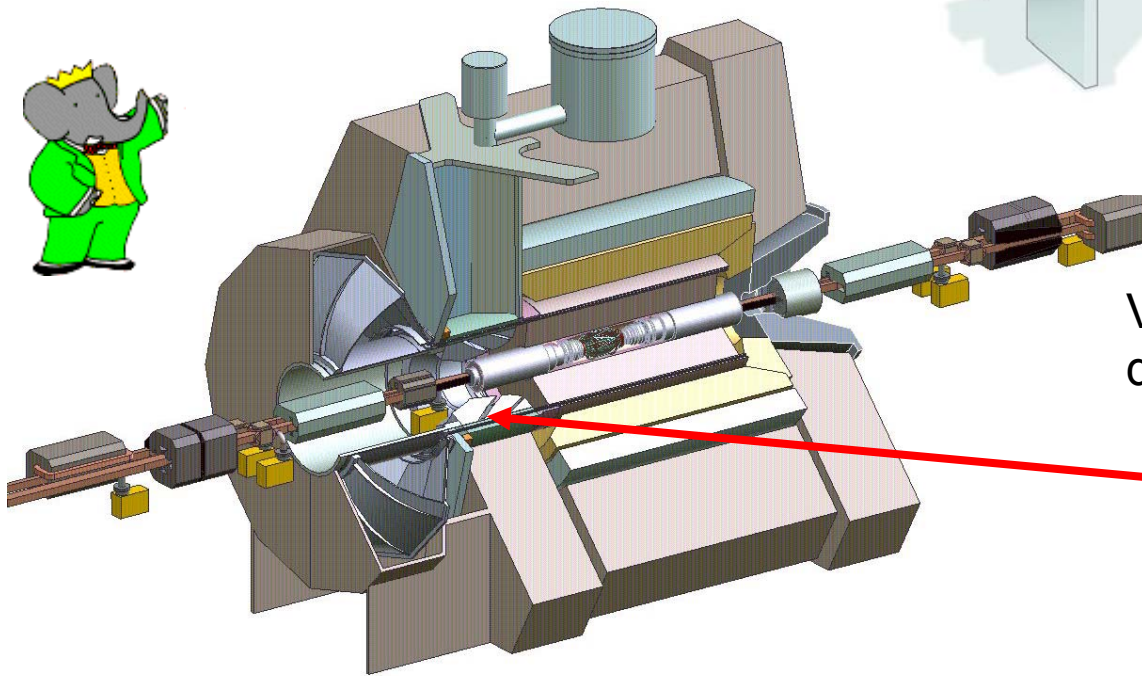
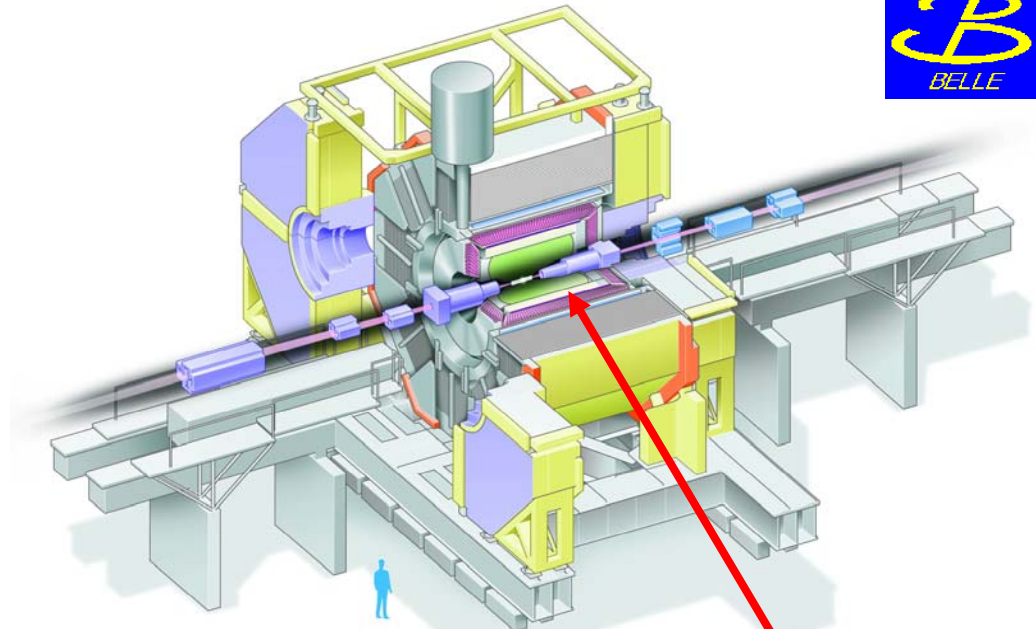
PEP-II tunnel: 2.2km in circumference



BaBar and Belle detectors

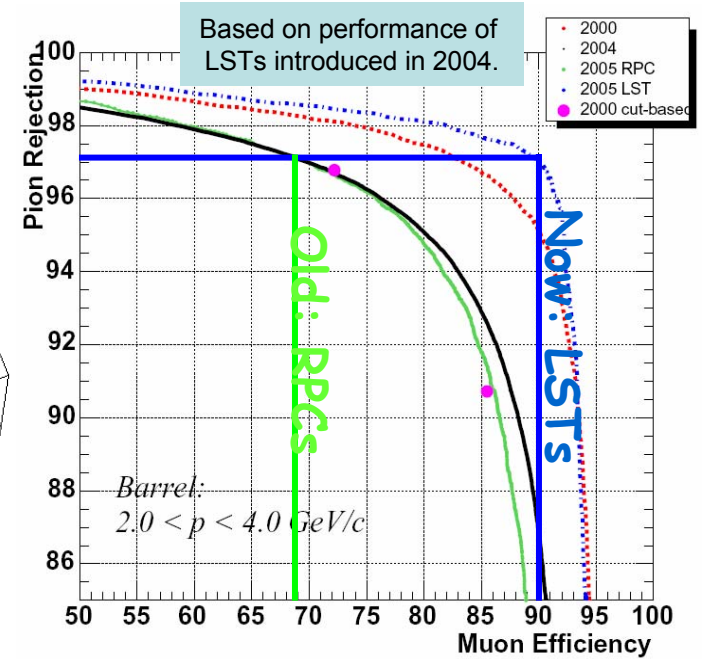
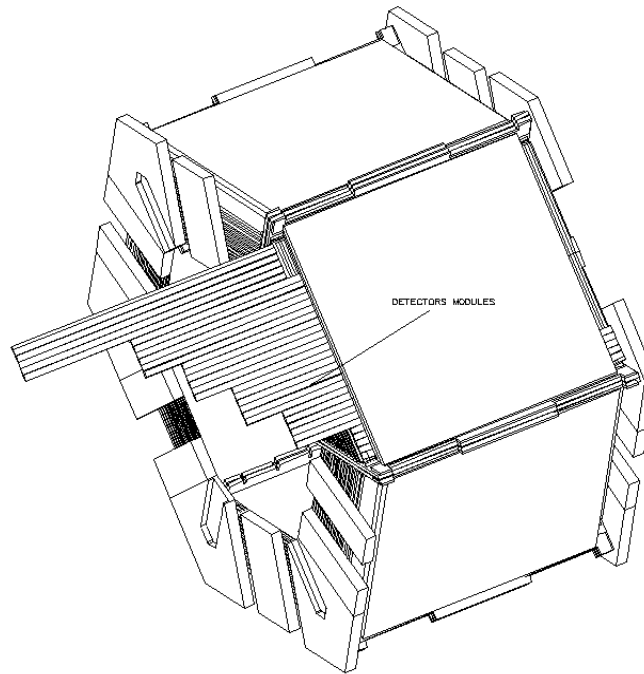


- BaBar recently upgraded its muon system and DCH electronics.

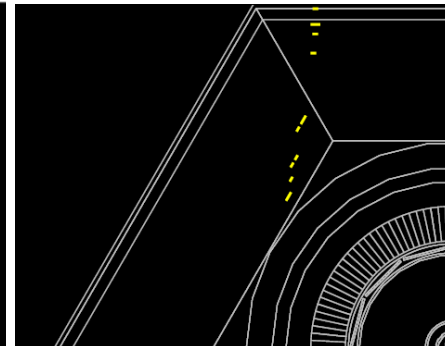
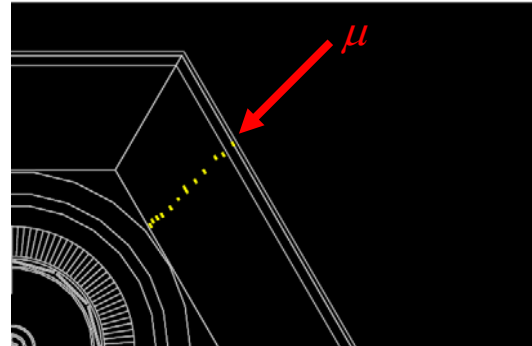
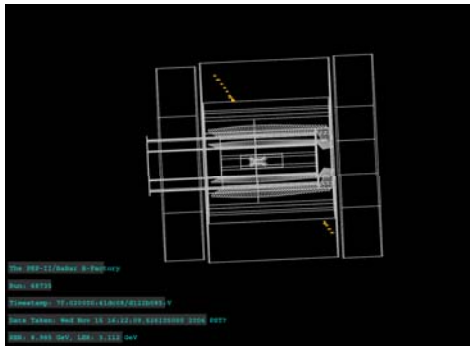


Very similar detectors. Main difference is PID:
Belle: Aerogel Cherenkov & ToF
BaBar: DIRC

IFR upgrade to LSTs

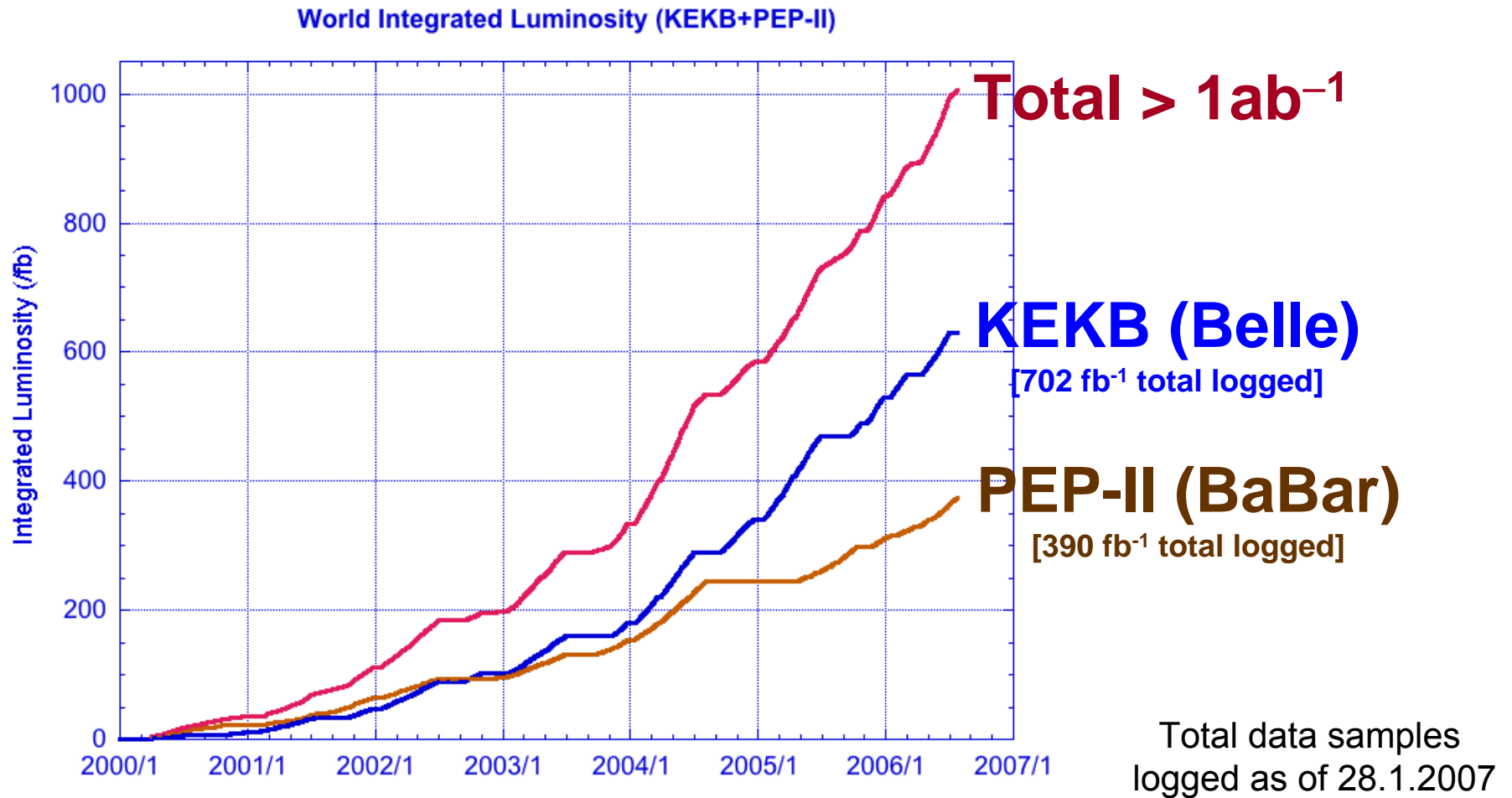


**Bottom & top LST sextants installed summer 2004.
 Remaining LST sextants installed autumn 2006.
 The fully upgraded LST system recorded its first cosmic rays November 2006**



Integrated luminosity

- B-factories have recorded over 10^9 B-pairs
- Dataset will double by the end of the program.

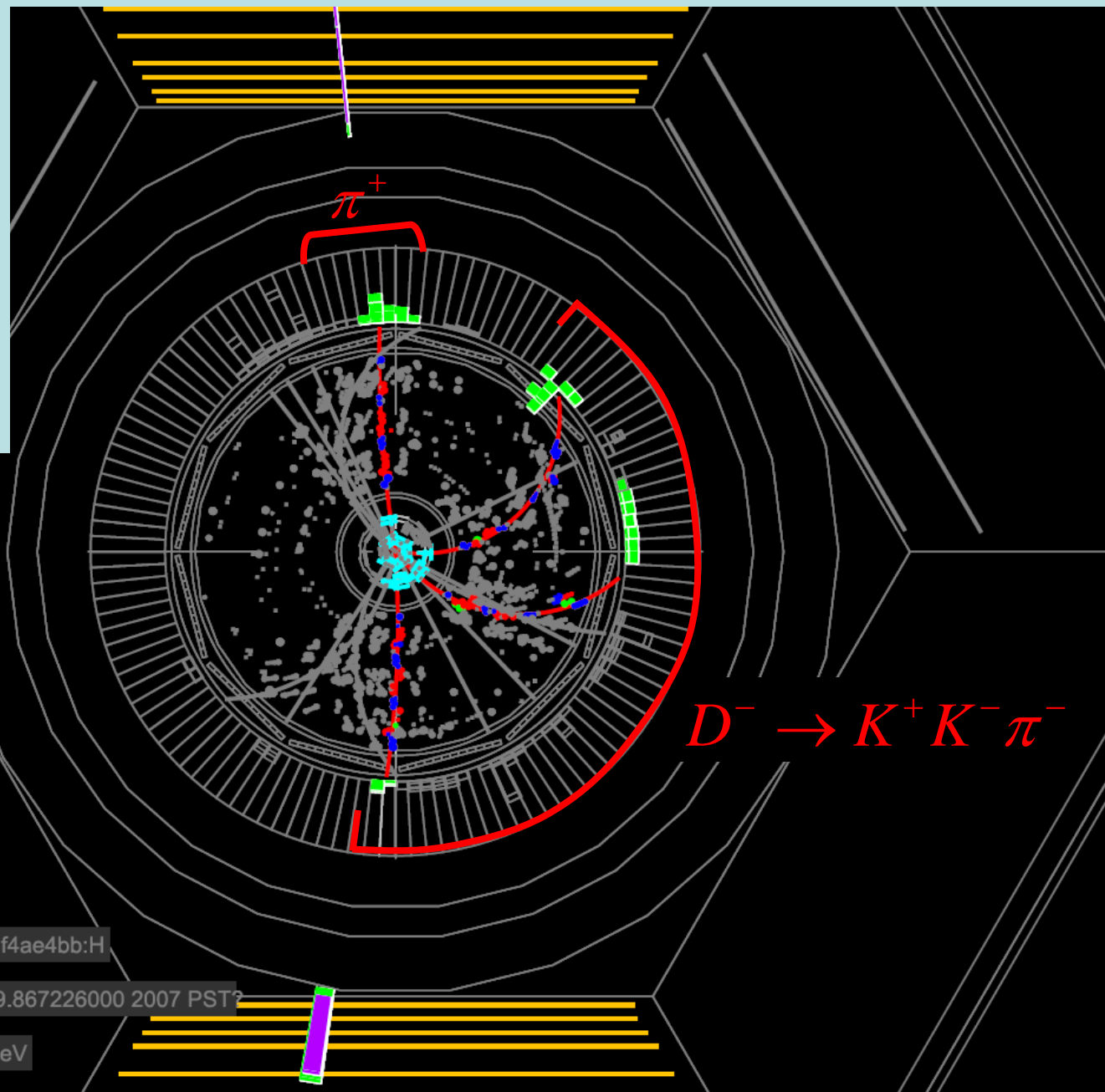


BaBar is taking data again

This event display shows the first fully reconstructed B decay of run 6.



The grey hits are from the other B in the event.



The PEP-II/BaBar B-Factory

Run: 69572

Timestamp: 7f:4fff77ff:430a74/1f4ae4bb:H

Date Taken: Fri Jan 19 08:43:09.867226000 2007 PST?

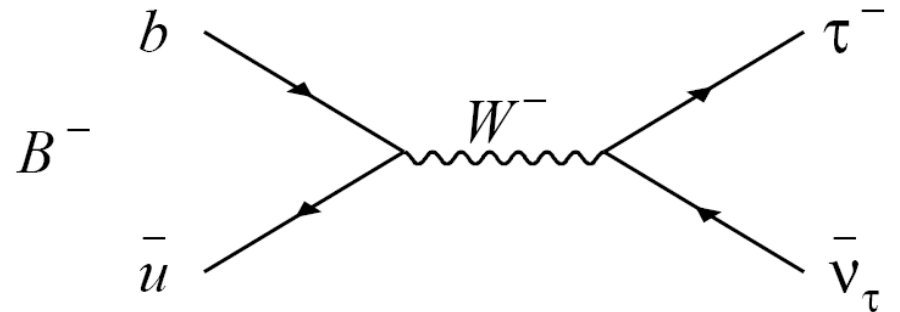
HER: 8.984 GeV, LER: 3.112 GeV

RESULTS

- (Semi-)Leptonic and radiative rare B decays
 - $B \rightarrow l\nu$
 - $B \rightarrow K^*ll$
 - $B \rightarrow d\gamma$

$B^+ \rightarrow \tau^+ \nu$

- Suppressed by V_{ub}

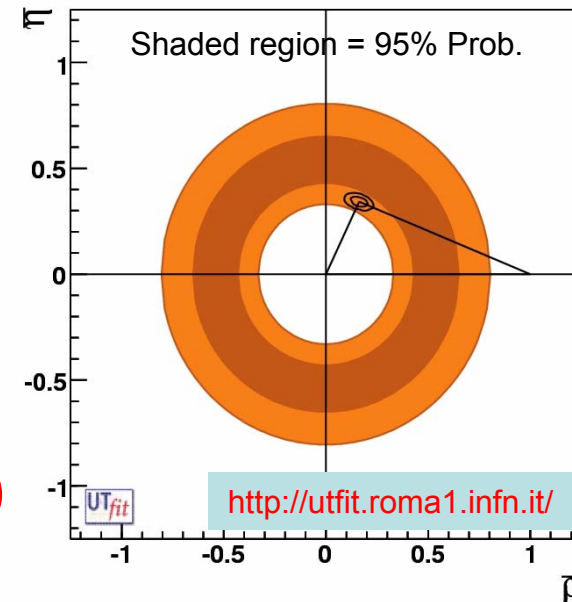


SM prediction
 $(1.59 \pm 0.40) \times 10^{-4}$



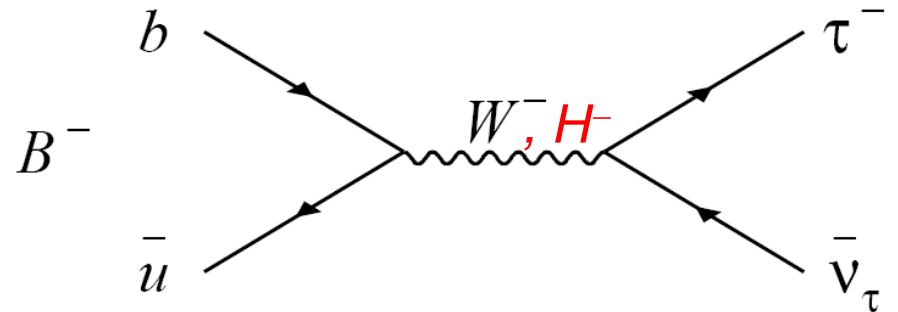
$$\mathcal{B}_{SM}(B^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 m_B m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_B^2}\right) f_B^2 |V_{ub}|^2 \tau_B$$

- Within the SM, this measurement can be used to constrain f_B .
- Can constrain the apex of the unitarity triangle using this measurement
 - Complements the angle measurements (Y.J. Kwon's talk this morning)



$B^+ \rightarrow \tau^+ \nu$

- Suppressed by V_{ub}



SM prediction
 $(1.59 \pm 0.40) \times 10^{-4}$



$$\mathcal{B}_{SM}(B^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 m_B m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_B^2}\right) f_B^2 |V_{ub}|^2 \tau_B$$

- Within the SM, this measurement can be used to constrain f_B .
- Can replace W^+ with H^+
 - \mathcal{B} can be suppressed or enhanced by a factor of r_H

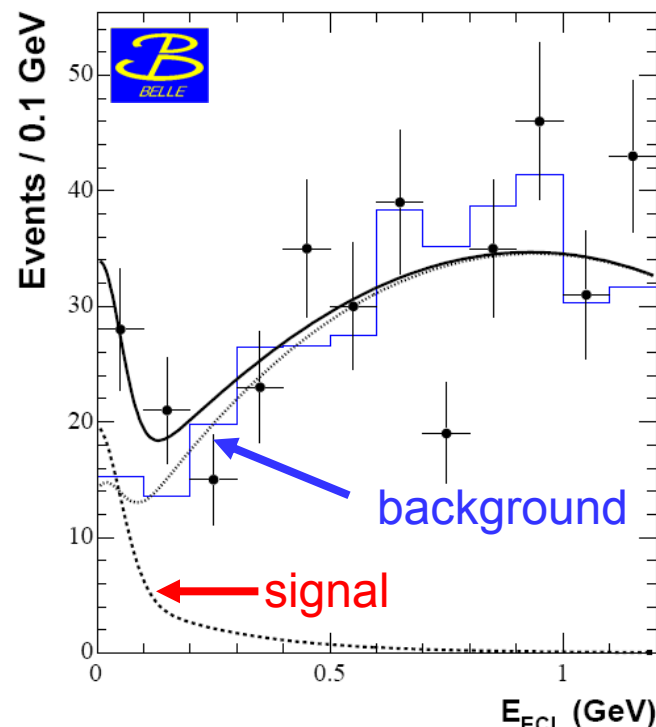
$$r_H = \left(1 - \frac{m_B^2}{m_H^2} \tan^2 \beta\right)^2$$

2HDM: W.S. Hou, PRD 48, 2342 (1993).

$B^+ \rightarrow \tau^+ \nu$

hep-ex/0608019
PRL97 (2006) 251802

- Reconstruct signal decay.
- and other B in the event:
 - Belle: fully reconstruct B mesons in 180 channels.
 - BaBar: Tag with $B \rightarrow D^{(*)} l \nu$.
- Look at the remaining energy in the calorimeter: signal peaks at $E_{\text{ECL/extra}} = 0$.



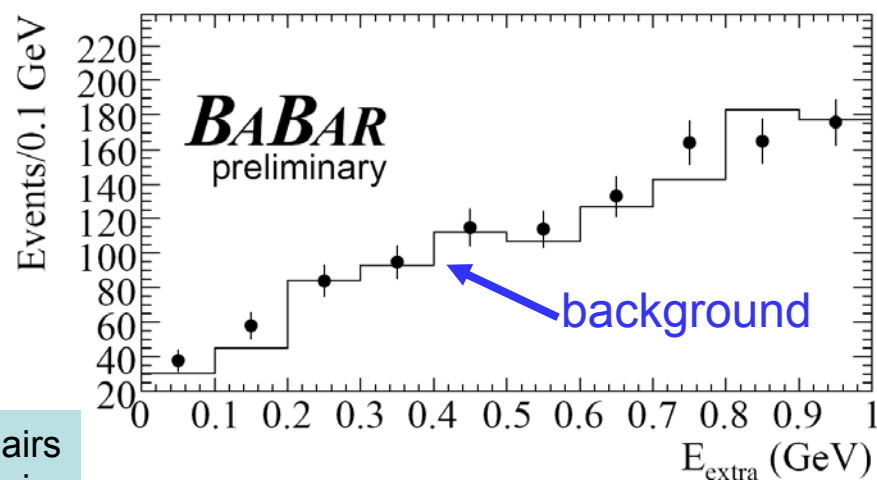
$$\mathcal{B} = (1.79_{-0.49-0.46}^{+0.56+0.39}) \times 10^{-4}$$

(revised). 3.5σ significance



$$\mathcal{B} = (0.88_{-0.67}^{+0.68} \pm 0.11) \times 10^{-4}$$

$$\text{BF} < 1.80 \times 10^{-4} @ 90\% \text{CL}$$



KEKCT '07

BaBar: 320×10^6 B pairs
Belle: 449×10^6 B pairs

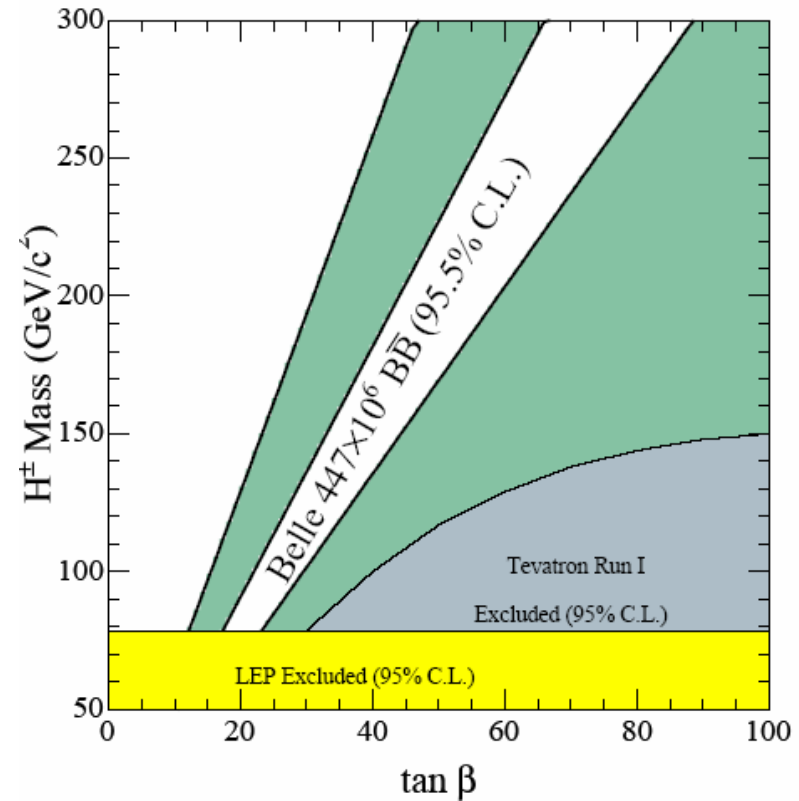
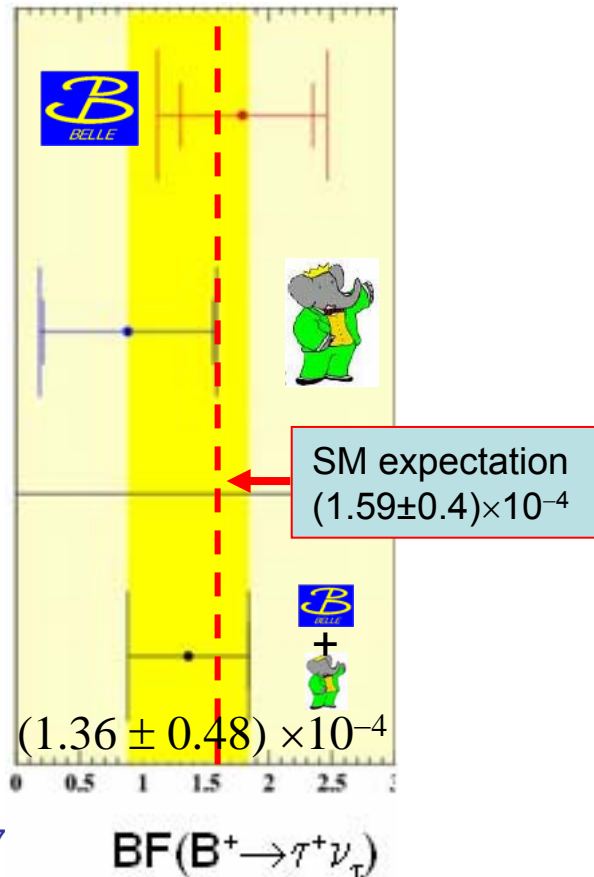
Constraints from $B^+ \rightarrow \tau^+ \nu$

hep-ex/0608019
PRL97 (2006) 251802

e.g. the 2HDM of W.S. Hou, PRD **48**, 2342 (1993).

- SM prediction can be enhanced/reduced by

a factor r_H : $r_H = \left(1 - \frac{m_B^2}{m_H^2} \tan^2 \beta\right)^2$



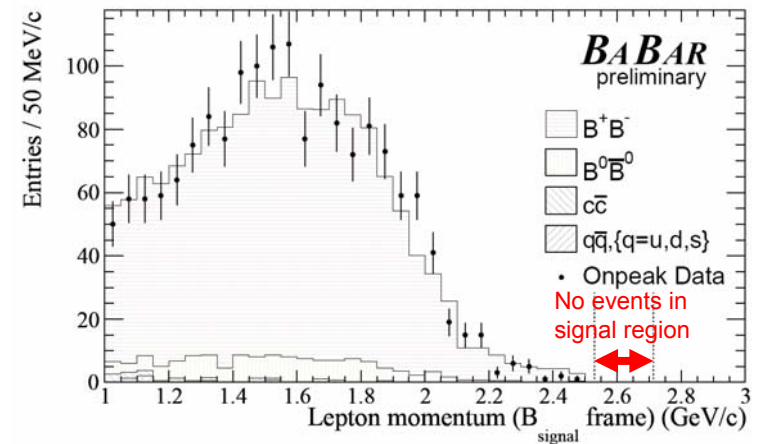
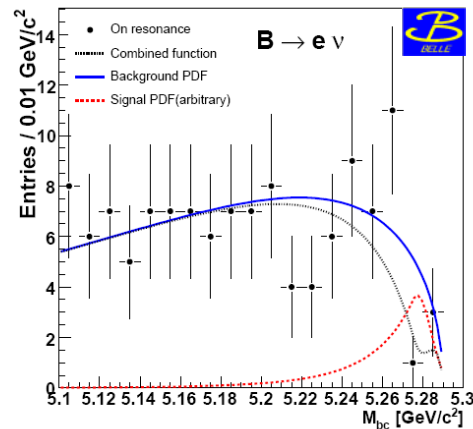
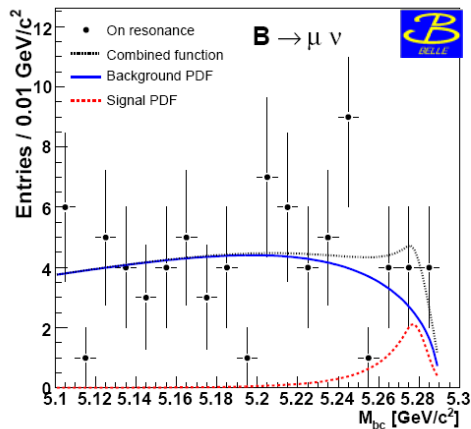
$B^+ \rightarrow e^+ \nu, \mu^+ \nu$

hep-ex/0607110
hep-ex/0611045

- Same physics motivation as $\tau^+ \nu$.

BaBar: 229×10^6 B pairs
Belle: 277×10^6 B pairs

$$\mathcal{B}_{SM}(B^+ \rightarrow l^+ \nu_l) = \frac{G_F^2 m_B m_l^2}{8\pi} \left(1 - \frac{m_l^2}{m_B^2}\right) f_B^2 |V_{ub}|^2 \tau_B$$



- These searches give null results. Upper limits are shown for **BaBar** and **Belle**.
- Consistent with SM.
- Best limits within a factor of 2 of SM

$$\mathcal{B}(B^+ \rightarrow e^+ \nu_e) < 7.9 \times 10^{-6} \text{ (90\% CL)}$$

$$\mathcal{B}(B^+ \rightarrow e^+ \nu_e) < 9.8 \times 10^{-7} \text{ (90\% CL)}$$

$$\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu) < 6.2 \times 10^{-6} \text{ (90\% CL)}$$

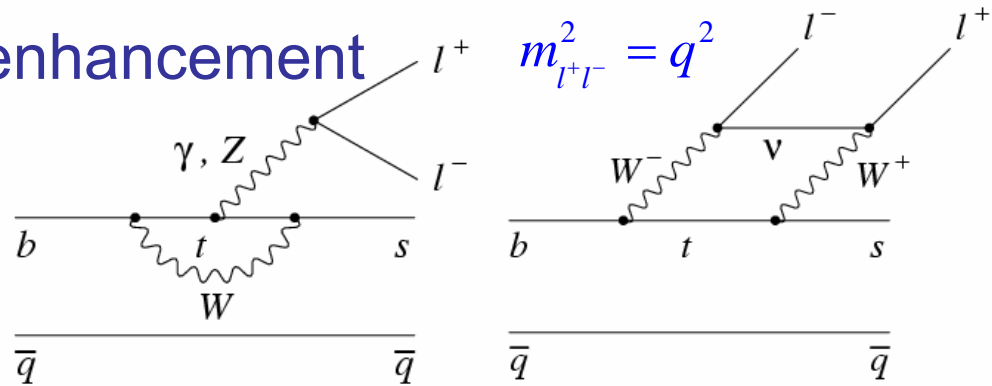
$$\mathcal{B}(B^+ \rightarrow \mu^+ \nu_\mu) < 1.7 \times 10^{-6} \text{ (90\% CL)}$$

B → K(*) II

F. Kruger, et al. PRD61 114028 (2000), Erratum D63 019901 (2001); F. Kruger, E. Lunghi PRD 63 014013 (2001); G. Hiller & F. Kruger PRD63 014013 (2001); Q. Yan et al PRD62 094023 (2000). etc.

- Flavor Changing Neutral Current, sensitive to NP in loops.
- $A_{CP}=0$ in SM can get NP enhancement

$$\mathcal{A}_{CP} = \frac{\bar{N} - N}{\bar{N} + N}$$



- $$R_K = \frac{\Gamma(B \rightarrow K \mu\mu)}{\Gamma(B \rightarrow Kee)} = 1.0000 \pm 0.0001 \text{ (SM)}$$

$$R_{K^*} = \frac{\Gamma(B \rightarrow K^* \mu\mu)}{\Gamma(B \rightarrow K^* ee)} \approx 0.75 \text{ to } 1.0 \text{ depending on } q^2 \text{ region (SM)}$$

- $R_{K^{(*)}}$ can be enhanced for Higgs doublet models with large $\tan\beta$.

- The forward backward asymmetry A_{FB} in the differential decay rate g , has a SM distribution as a function of q^2 , deviations from this indicate NP.

$$A_{FB}(q^2) = \frac{\int_{-1}^1 \text{sgn}(\cos \theta) g(q^2, \theta) d \cos \theta}{\int_{-1}^1 g(q^2, \theta) d \cos \theta}$$

- θ is the angle between the lepton (+/-) momentum and B (\bar{B}/B) in the dilepton rest frame

B → K^(*) II

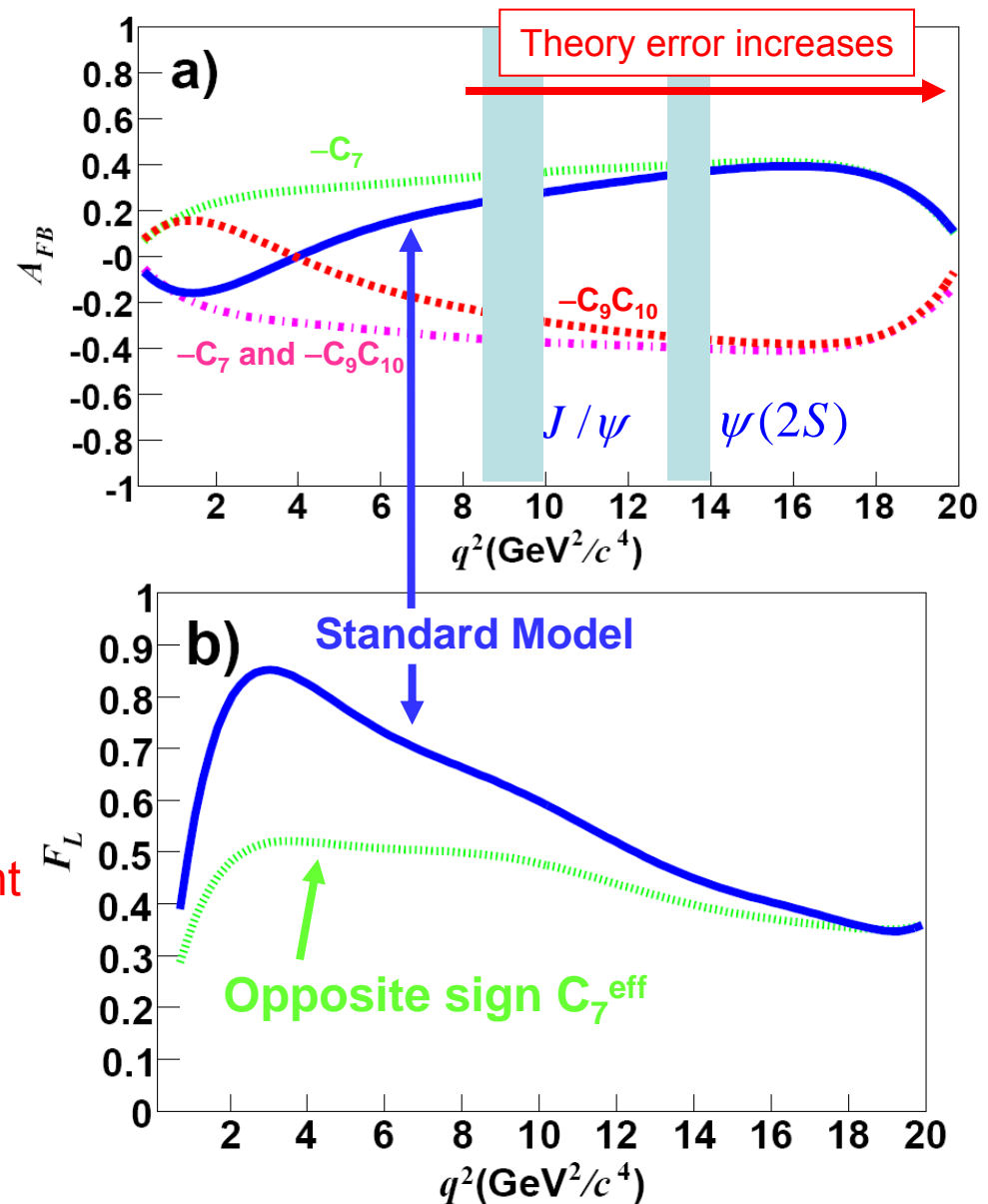
Figures from PRD73 (2006) 092001

- Shape of $A_{FB}(q^2)$ can be used to test SM
 - measure effective parameters related to Wilson coefficients C_j .

C_7	– γ electroweak penguin
C_9	– Z^0 electroweak penguin
C_{10}	– box diagram

- K^{*II} has $F_L(q^2)$
 - F_L = fraction of longitudinally polarised events.
 - Deviations from SM expectations can signal right handed currents.

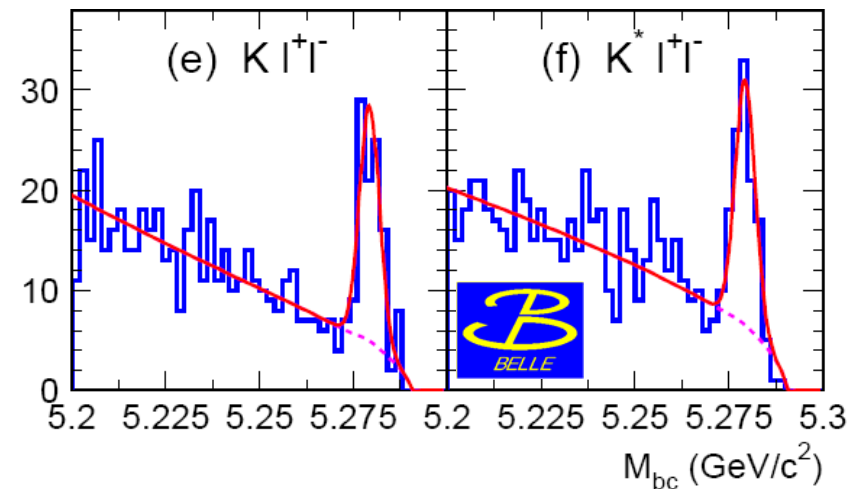
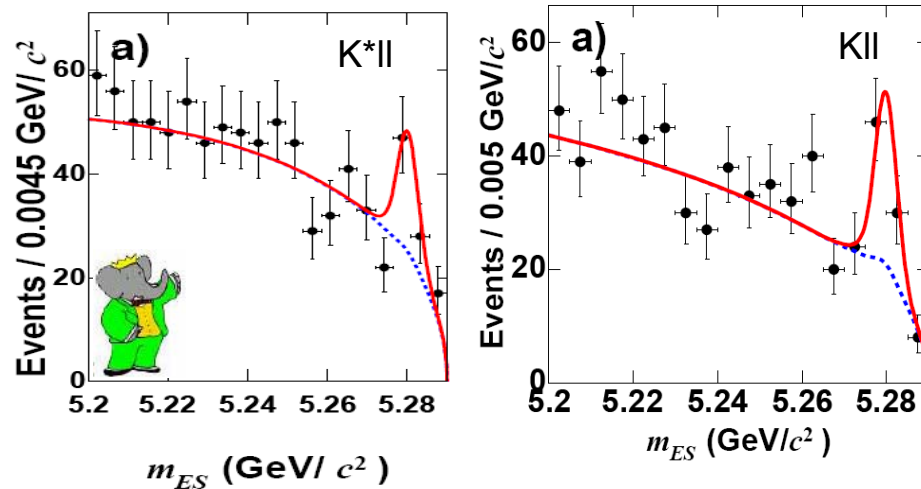
A. Ali et al. PRD66 034002 (2002); PRD61 074024 (200); F. Kruger & J. Matias PRD71 094009 (2005).



B → K(*)ll

hep-ex/0410006
PRD73 (2006) 092001

- These modes have the smallest measured branching fraction of any observed B decay.



$$\mathcal{B}(B \rightarrow Kll) = (0.34 \pm 0.07 \pm 0.02) \times 10^{-6}$$

$$\mathcal{B}(B \rightarrow K^*ll) = (0.78^{+0.19}_{-0.17} \pm 0.11) \times 10^{-6}$$

$$R_K = 1.06 \pm 0.48 \pm 0.08$$

$$R_{K^*} = 0.91 \pm 0.45 \pm 0.06$$

$$\mathcal{A}_{CP}(B \rightarrow Kll) = -0.07 \pm 0.22 \pm 0.02$$

$$\mathcal{A}_{CP}(B \rightarrow K^*ll) = 0.03 \pm 0.23 \pm 0.03$$

$$\mathcal{B}(B \rightarrow Kll) = (0.55 \pm 0.07 \pm 0.03) \times 10^{-6}$$

$$\mathcal{B}(B \rightarrow K^*ll) = (1.65^{+0.23}_{-0.22} \pm 0.10) \times 10^{-6}$$

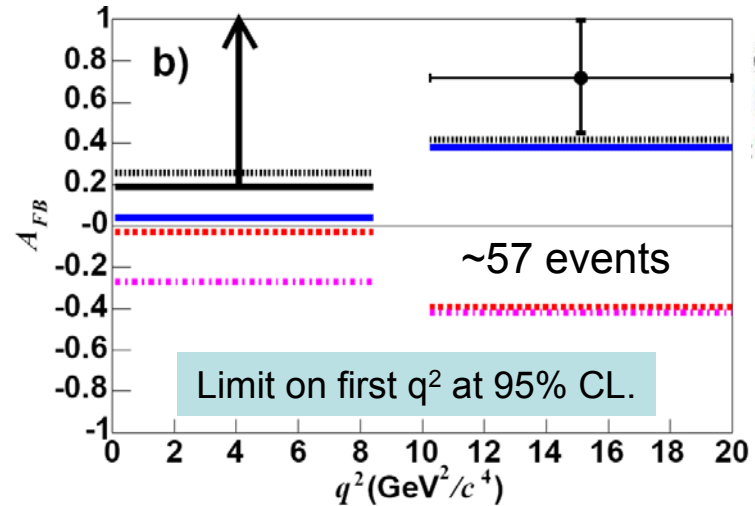
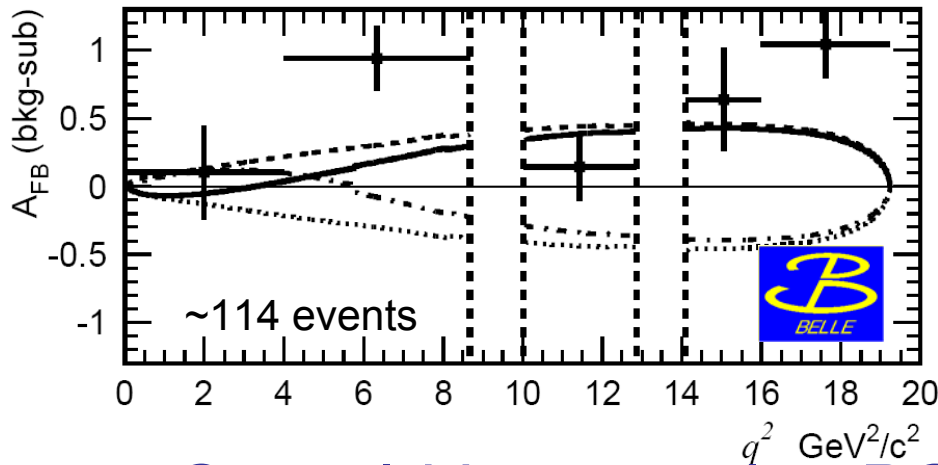
$$R_K = 1.38 \pm 0.40 \pm 0.07$$

$$R_{K^*} = 0.98 \pm 0.30 \pm 0.08$$

B → K(*) II

PRL96 (2006) 251801
PRD73 (2006) 092001

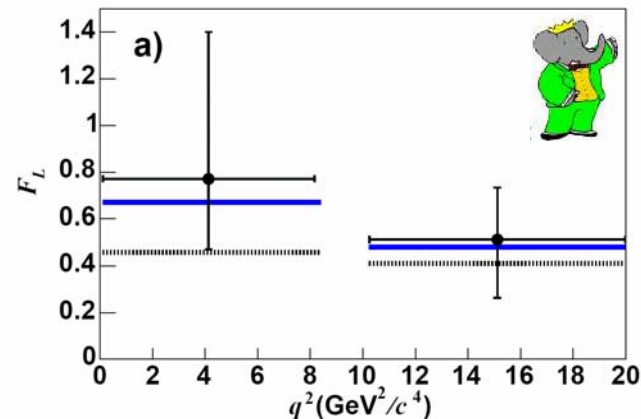
- First A_{FB} measurements from the B-factories are compatible with SM.



- C_i could be complex BSM: should test this in the future. [A. Hovhannisyan et al. hep-ph/0701046](#), [A. Cornell et al. hep-ph/0505136](#)

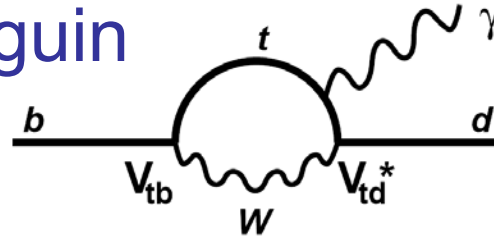
- Also measured F_L to be compatible with SM

BaBar: 229×10^6 B pairs
Belle: 386×10^6 B pairs

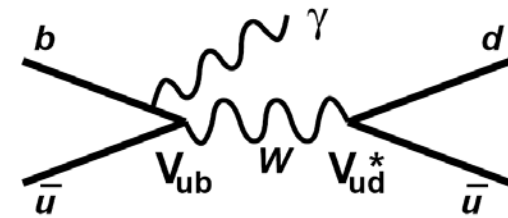


B → dγ transitions: ωγ, ργ

- Radiative penguin decay



B⁰ and B[±] decays



Only B[±] decays

- The ratio of dγ/K*γ measures |V_{td}/V_{ts}|.

$$\frac{\mathcal{B}[B \rightarrow (\rho/\omega)\gamma]}{\mathcal{B}(B \rightarrow K^*\gamma)} = \left| \frac{V_{td}}{V_{ts}} \right|^2 \left(\frac{1 - m_\rho^2/M_B^2}{1 - m_{K^*}^2/M_B^2} \right)^3 \zeta^2 [1 + \Delta R].$$

Difference in decay dynamics

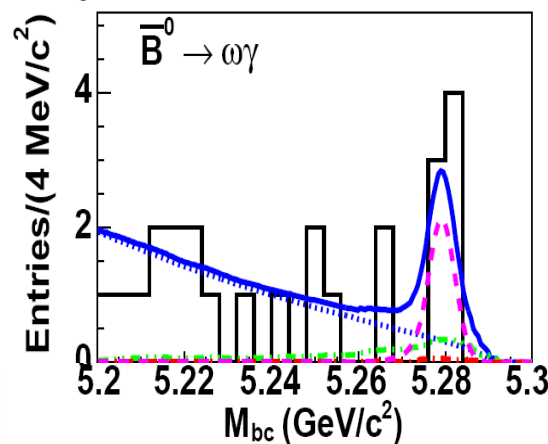
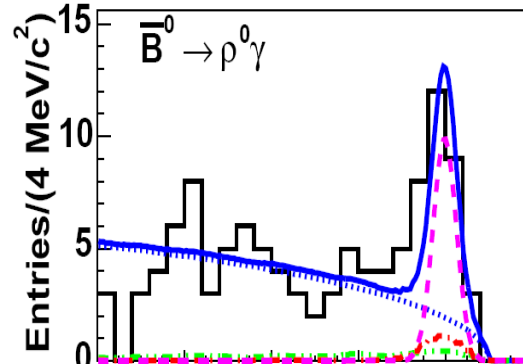
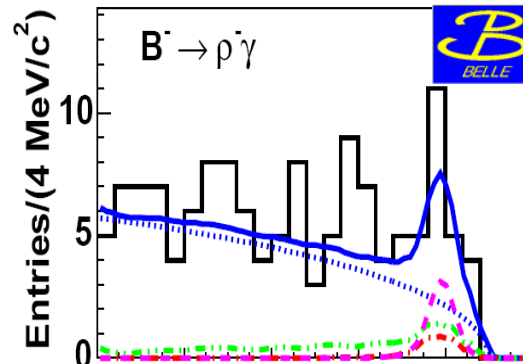
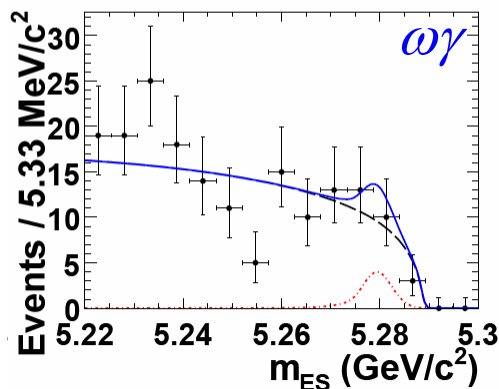
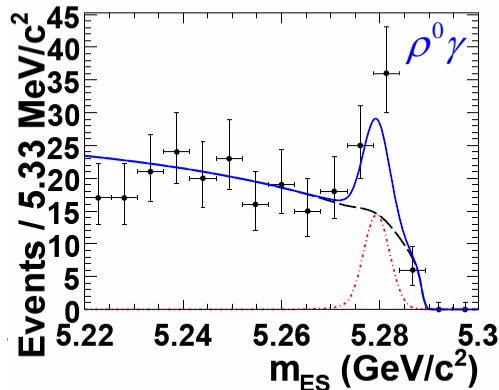
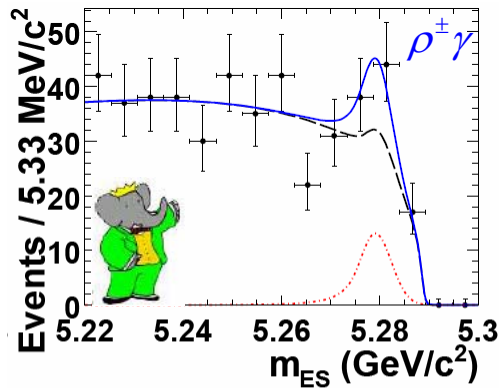
Ratio of form factors

- Any inconsistency between this and the constraint from $\Delta m_d/\Delta m_s$ would indicate new physics.
 - CDF measure $|V_{td}/V_{ts}| = 0.2060 \pm 0.0007$ (exp) ± 0.007 (th)

CDF Collaboration hep-ex/0609040

B → dγ transitions: ωγ, ργ

RPL96 (2006) 221601
hep-ex/0612017



BaBar: 347×10^6 B pairs
Belle: 386×10^6 B pairs

- Both experiments observe $b \rightarrow d\gamma$ decays.
- With very consistent results.

$$\mathcal{B}(B \rightarrow \rho\gamma, \omega\gamma) = (1.25 \pm 0.25 \pm 0.09) \times 10^{-6}$$

$$\frac{\mathcal{B}(B \rightarrow \rho\gamma, \omega\gamma)}{\mathcal{B}(B \rightarrow K^* \gamma)} = 0.030 \pm 0.006$$

$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.200 \pm 0.020 \pm 0.015$$



$$\mathcal{B}(B \rightarrow \rho\gamma, \omega\gamma) = (1.32^{+0.34}_{-0.31} \pm 0.10) \times 10^{-6}$$

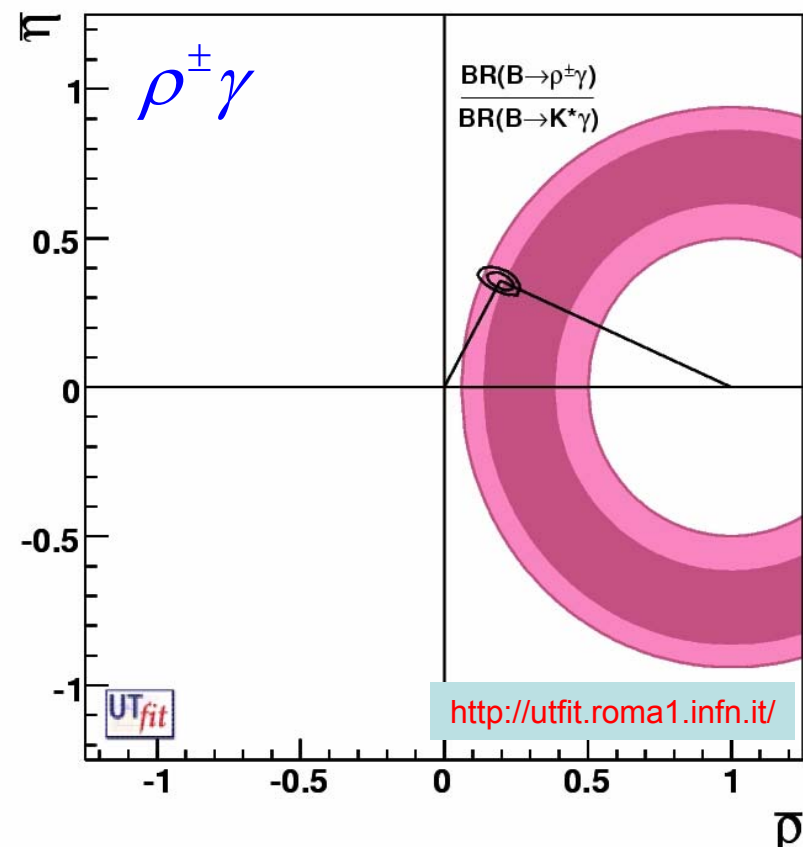
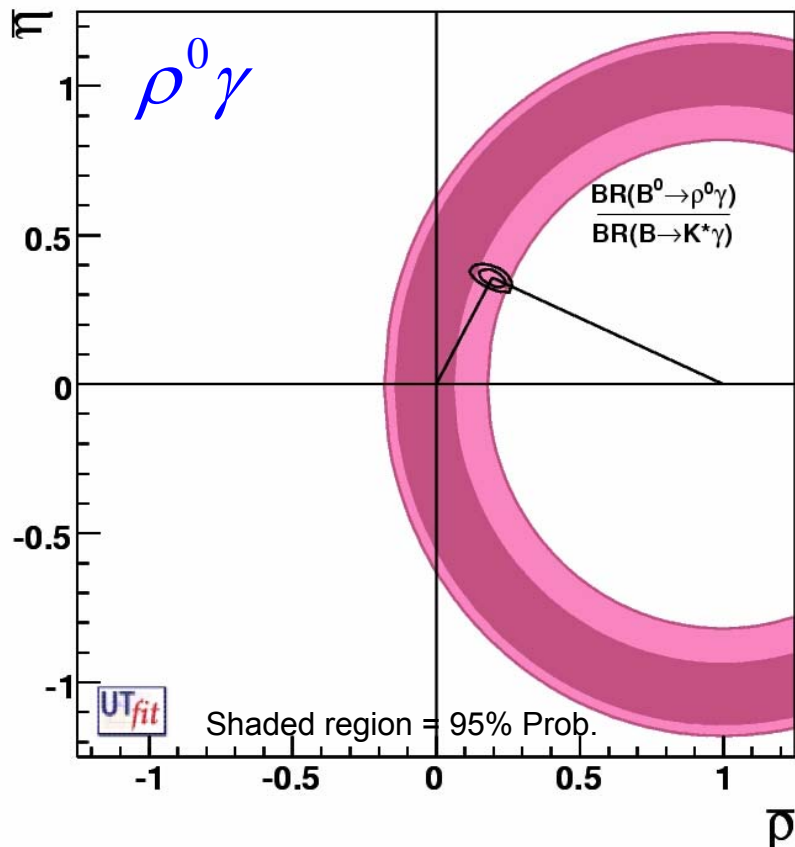
$$\frac{\mathcal{B}(B \rightarrow \rho\gamma, \omega\gamma)}{\mathcal{B}(B \rightarrow K^* \gamma)} = 0.032 \pm 0.006 \pm 0.002$$

$$\left| \frac{V_{td}}{V_{ts}} \right| = 0.199 \pm 0.026^{+0.018}_{-0.015}$$



B \rightarrow d γ transitions: $\omega\gamma$, $\rho\gamma$

- Can constrain the unitarity triangle using B \rightarrow K* γ
 - Orthogonal to constraint from B $^+\rightarrow\tau^+\nu$
 - Compliments angle measurements (Y.J. Kwon's talk this morning)

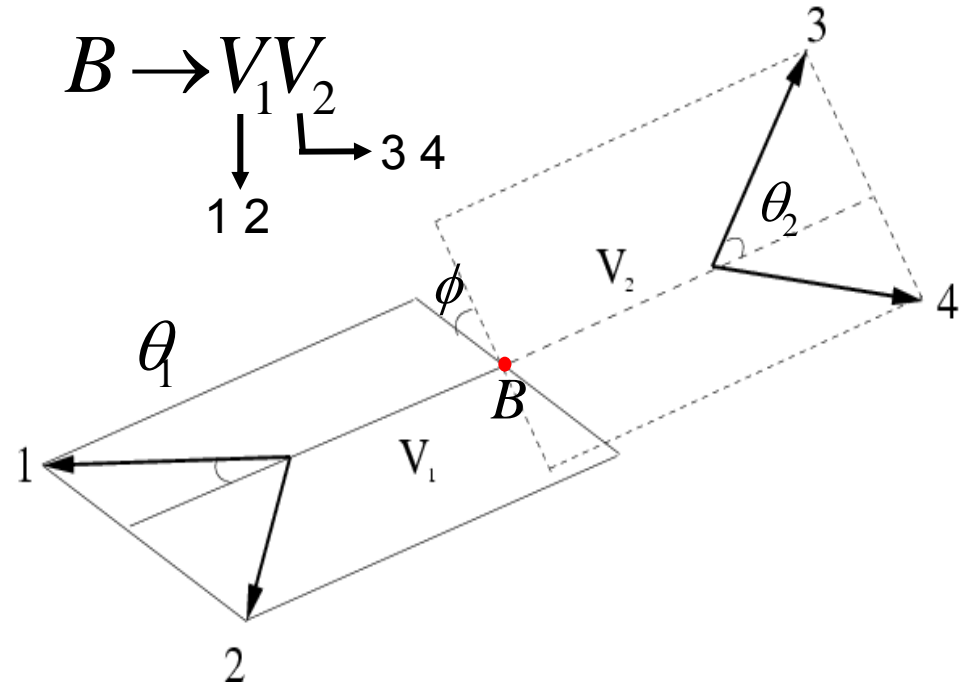


RESULTS

- Charmless hadronic rare B decays.
 - $B \rightarrow K^* \rho$
 - $B^0 \rightarrow a_1 \rho$
 - $B^+ \rightarrow \rho^+ \pi^0$
 - Direct CP Violation searches

B → VV decays

- 11 observables
 - 6 amplitudes, $A_0, A_{+1}, A_{-1} + \text{C.C.}$
 - 5 phases
- Simplify analysis to separating transverse and longitudinal events when have low statistics.
 - Measure polarisation: f_L
- Analogous to $B \rightarrow K^* \Pi$ and $H \rightarrow ZZ \rightarrow l^+ l^- l^+ l^-$



$$\frac{d^3\Gamma}{d \cos \theta_1 d \cos \theta_2 d\Phi} \propto \left| \sum_{m=-1,0,1} A_m Y_{1,m}(\theta_1, \Phi) Y_{1,-m}(\theta_2, \Phi) \right|^2$$

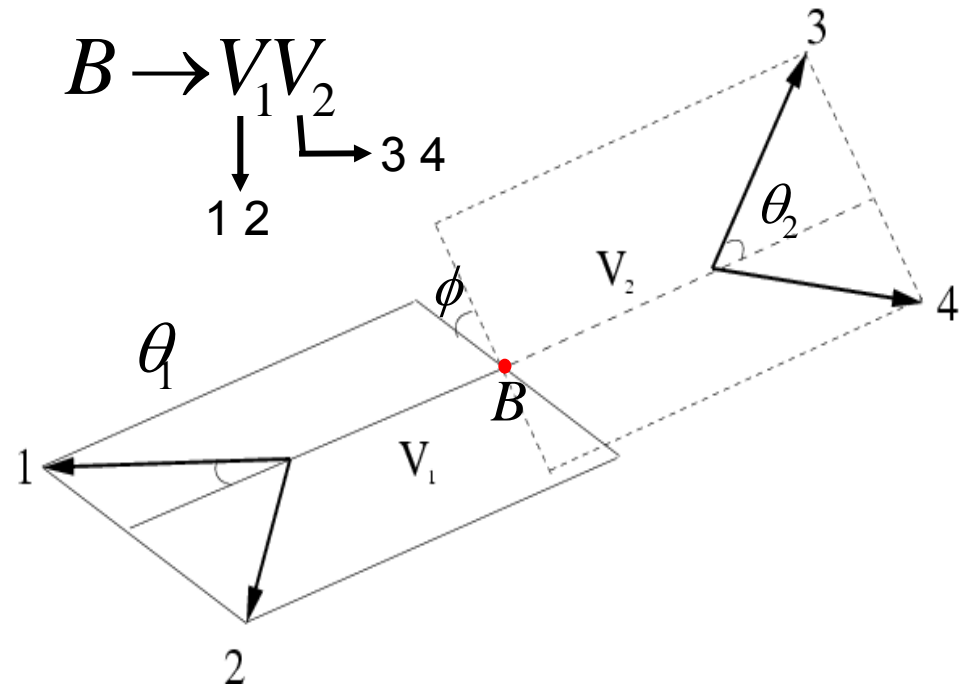
$$\propto \left\{ \begin{aligned} & \frac{1}{4} \sin^2 \theta_1 \sin^2 \theta_2 (|A_{+1}|^2 + |A_{-1}|^2) + \cos^2 \theta_1 \cos^2 \theta_2 |A_0|^2 \\ & + \frac{1}{2} \sin^2 \theta_1 \sin^2 \theta_2 [\cos 2\Phi \Re(A_{+1} A_{-1}^*) - \sin 2\Phi \Im(A_{+1} A_{-1}^*)] \\ & + \frac{1}{4} \sin 2\theta_1 \sin 2\theta_2 [\cos \Phi \Re(A_{+1} A_0^* + A_{-1} A_0^*) - \sin \Phi \Im(A_{+1} A_0^* - A_{-1} A_0^*)] \end{aligned} \right\}$$

$$f_L = \frac{|A_0|^2}{\sum_{m=-1,0,1} |A_m|^2}$$

Integrate over $\Phi \dots$

B → VV decays

- 11 observables
 - 6 amplitudes, $A_0, A_{+1}, A_{-1} + \text{C.C.}$
 - 5 phases
- Simplify analysis to separating transverse and longitudinal events when have low statistics.
 - Measure polarisation: f_L
- Analogous to $B \rightarrow K^* \Pi$ and $H \rightarrow ZZ \rightarrow l^+ l^- l^+ l^-$



$$\frac{d^3\Gamma}{d \cos \theta_1 d \cos \theta_2} \propto \left\{ f_L \cos^2 \theta_1 \cos^2 \theta_2 + \frac{1}{4} (1 - f_L) \sin^2 \theta_1 \sin^2 \theta_2 \right\}$$

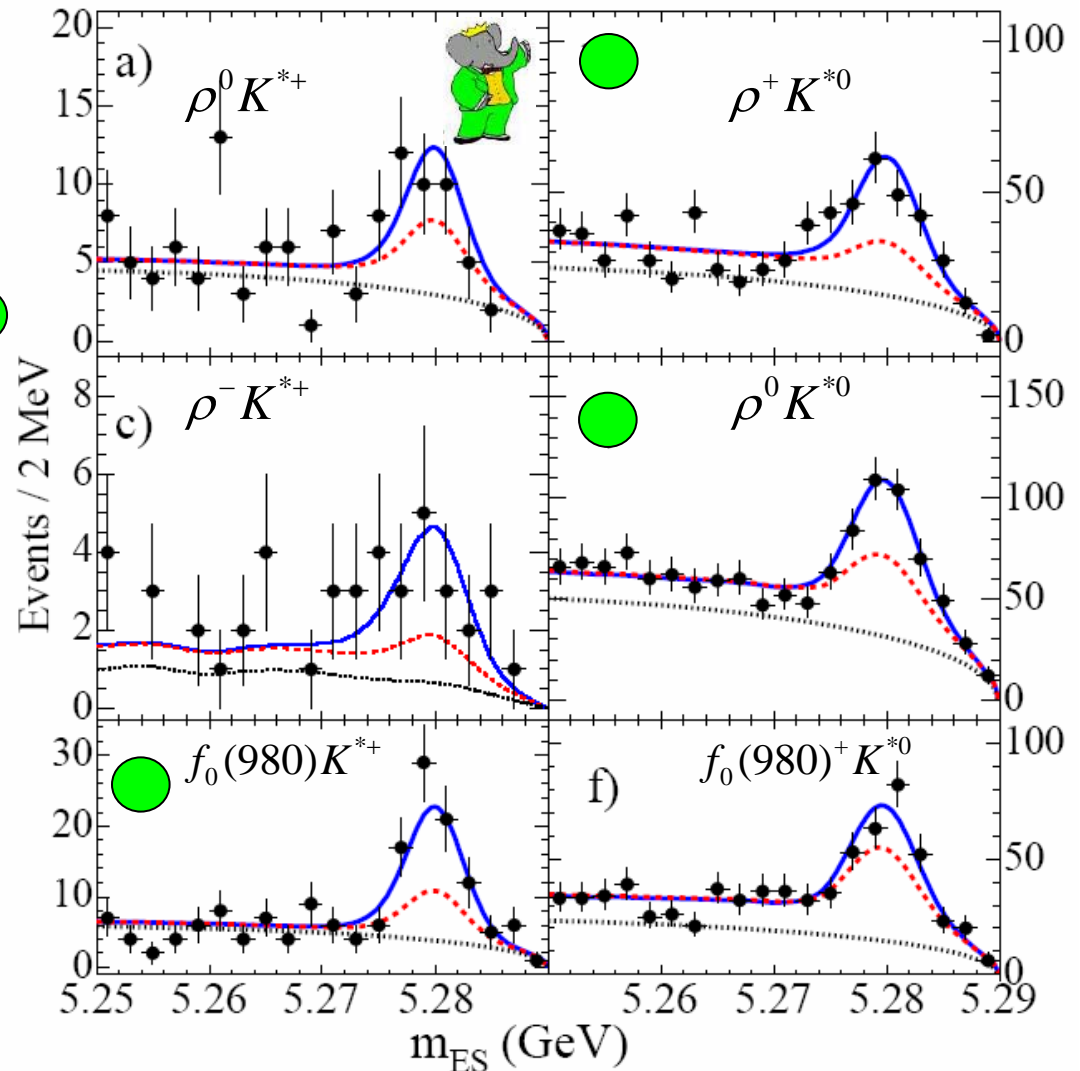
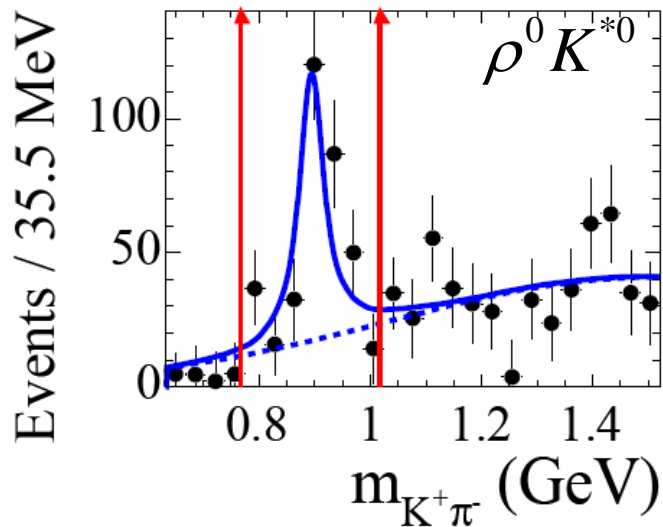
$$f_L = \frac{|A_0|^2}{\sum_{m=-1,0,1} |A_m|^2}$$

.... to simplify the angular correlation.

$B \rightarrow K^* \rho$

PRL97 (2006) 201801

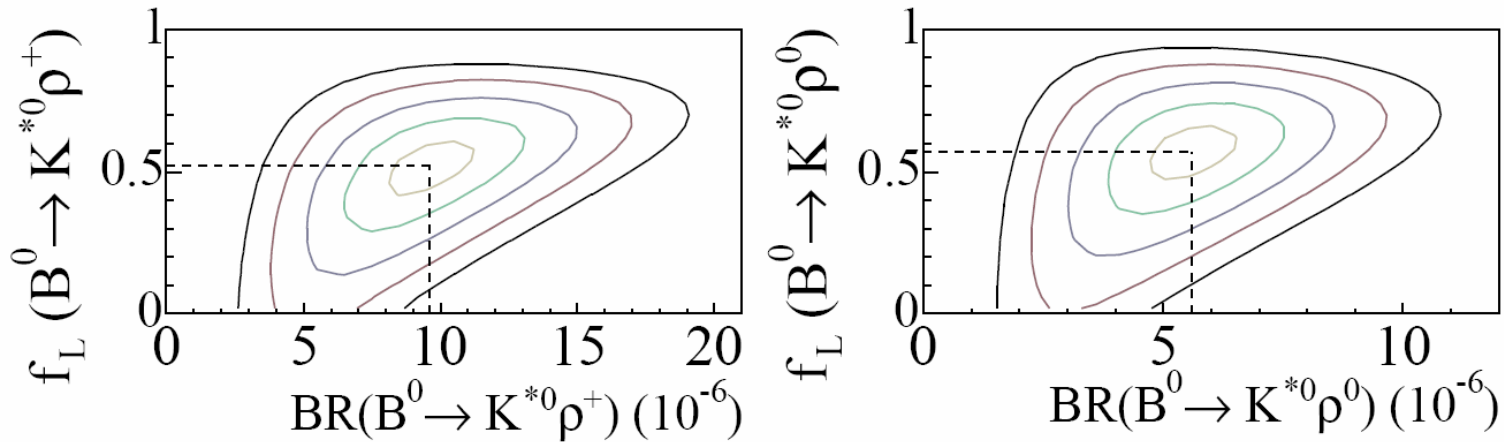
- 232×10^6 B Pairs
- $BF \sim \text{few } 10^{-6}$.
- 2 VV modes and $f_0 K^{*+}$ have been observed. ●
- Understanding non-resonant $K\pi$ background is critical for these analyses.



B → K* ρ

PRL97 (2006) 201801

- For penguins we expect $f_L \sim 0.5$, trees we expect $f_L \sim 1.0$.
- The interest is in trying to understand the underlying dynamics of these decays.



Mode	n_{sig}	$S(\sigma)$	$\mathcal{B}(10^{-6})$	f_L	\mathcal{A}_{CP}
$\rho^0 K^{*+}$		2.5	$3.6_{-1.6}^{+1.7} \pm 0.8$ (6.1)	$[0.9 \pm 0.2]$	–
$\rightarrow \rho^0 K^{*+}_{K^+\pi^0}$	19_{-15}^{+16}	1.3	$3.2_{-2.4}^{+2.7} \pm 0.9$	$[0.8_{-0.5}^{+0.3}]$	–
$\rightarrow \rho^0 K^{*+}_{K^0_S \pi^+}$	32_{-17}^{+19}	2.1	$3.8_{-2.1}^{+2.2} \pm 0.9$	$[1.0 \pm 0.3]$	–
$\rho^+ K^{*0}$	194 ± 29	7.1	$9.6 \pm 1.7 \pm 1.5$	$0.52 \pm 0.10 \pm 0.04$	$-0.01 \pm 0.16 \pm 0.02$
$\rho^- K^{*+}_{K^+\pi^0}$	60_{-22}^{+25}	1.6	$5.4_{-3.4}^{+3.8} \pm 1.6$ (12.0)	$[-0.18_{-1.74}^{+0.52}]$	–
$\rho^0 K^{*0}$	185 ± 30	5.3	$5.6 \pm 0.9 \pm 1.3$	$0.57 \pm 0.09 \pm 0.08$	$0.09 \pm 0.19 \pm 0.02$
$f_0(980) K^{*+}$		5.0	$5.2 \pm 1.2 \pm 0.5$	–	$-0.34 \pm 0.21 \pm 0.03$
$\rightarrow f_0(980) K^{*+}_{K^+\pi^0}$	40_{-12}^{+13}	3.8	$6.2_{-1.9}^{+2.1} \pm 0.7$	–	$-0.50 \pm 0.29 \pm 0.03$
$\rightarrow f_0(980) K^{*+}_{K^0_S \pi^+}$	37_{-12}^{+14}	3.2	$4.2_{-1.4}^{+1.5} \pm 0.5$	–	$-0.13 \pm 0.30 \pm 0.01$
$f_0(980) K^{*0}$	83 ± 19	3.5	$2.6 \pm 0.6 \pm 0.9$ (4.3)	–	$-0.17 \pm 0.28 \pm 0.02$

$B^+ \rightarrow K^{*0} \rho^+ / a_1 \rho$ & α from $\rho\rho$

PRL97 (2006) 201801
PRD74 (2006) 031104

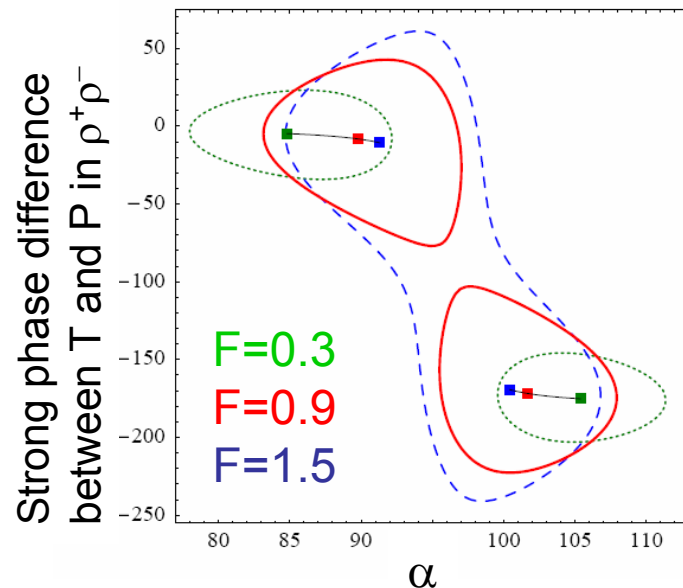
- $B^+ \rightarrow K^{*0} \rho^+$ is a pure penguin decay that can be related to the penguin amplitude in $B^0 \rightarrow \rho^+ \rho^-$.

Beneke et al., Phys.Lett. B638 (2006) 68-73

$$\mathcal{B}(B^+ \rightarrow K^{*0} \rho^+) = (9.6 \pm 1.7 \pm 1.5) \times 10^{-6}$$

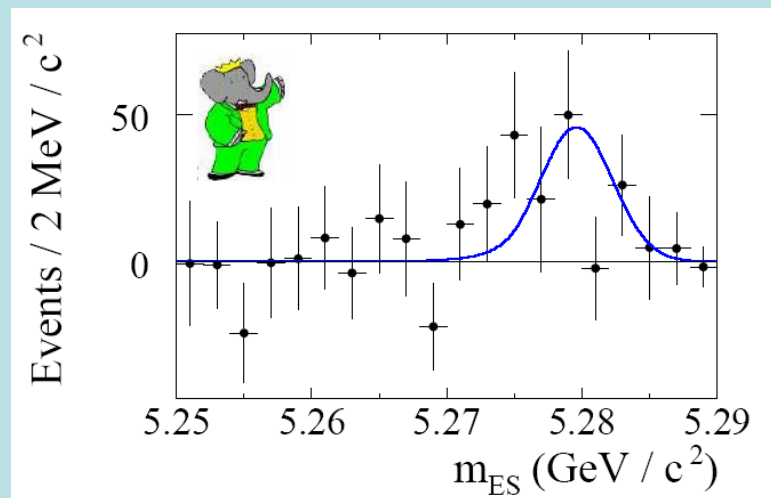
- This approach gives a more precise measurement of the unitarity triangle angle than traditional methods.

$$\sigma(\alpha) \sim 7^\circ (\text{expt.}) \pm 1.5^\circ (\text{th.})$$



- $a_1 \rho$ is a significant background to other rare decays like $\rho\rho$.
- Recent search provides useful upper limit on this decay.

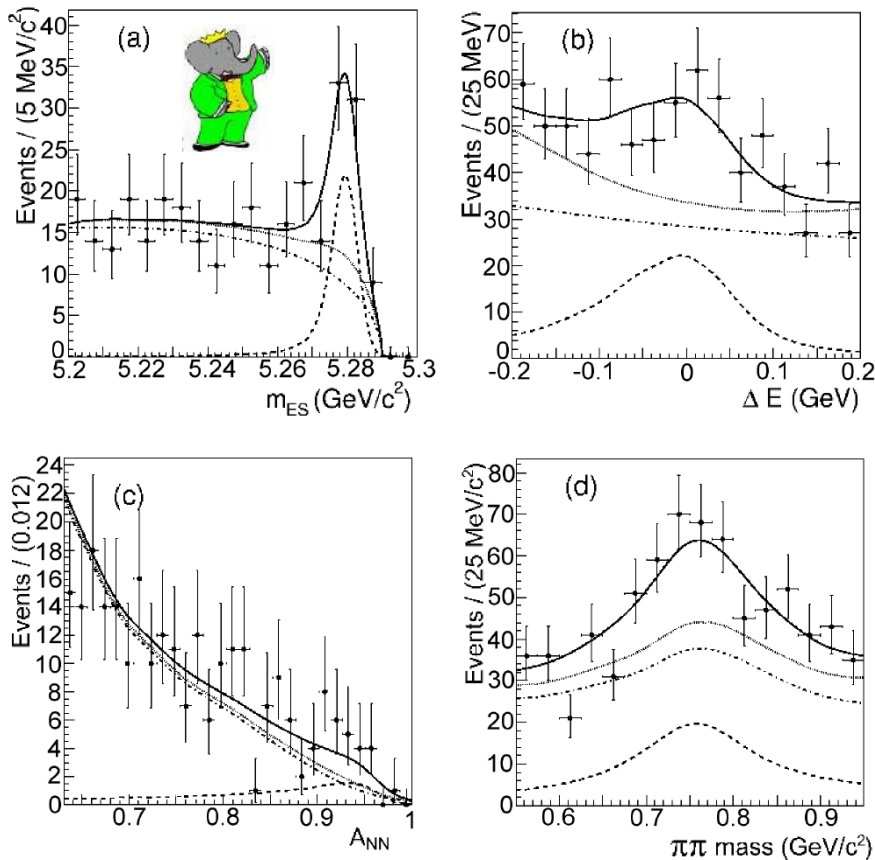
$$\mathcal{B}(B^0 \rightarrow a_1^\pm \rho^\mp) < 61 \times 10^{-6} \quad (90\% \text{ CL})$$



$B^+ \rightarrow \rho^+ \pi^0$

hep-ex/0701035

- Recently updated by BaBar using 227×10^6 B pairs



- Useful input for an isospin analysis of $B \rightarrow \rho\pi$ decays.
- Can also search for direct CP violation in this mode:

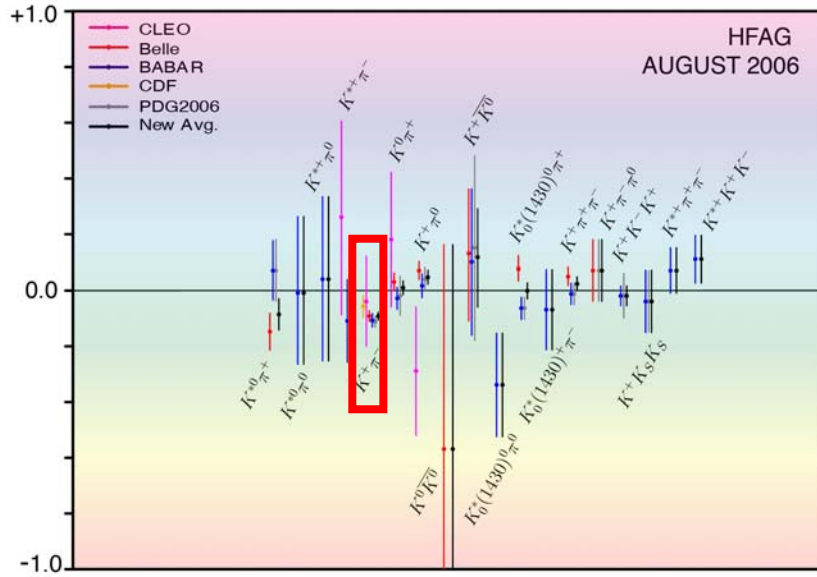
$$\mathcal{A}_{CP} = \frac{\bar{N} - N}{\bar{N} + N}$$

$$B(B^+ \rightarrow \rho^+ \pi^0) = (10.2 \pm 1.4 \pm 0.9) \times 10^{-6}$$

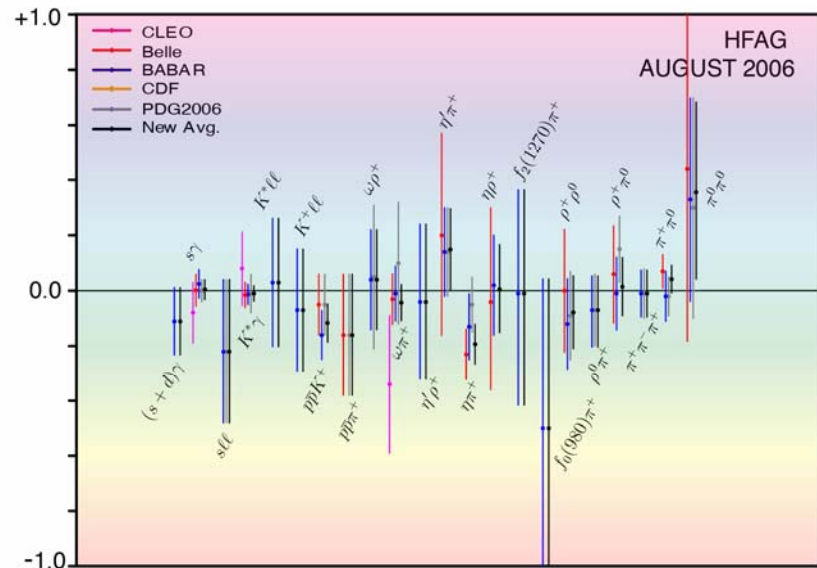
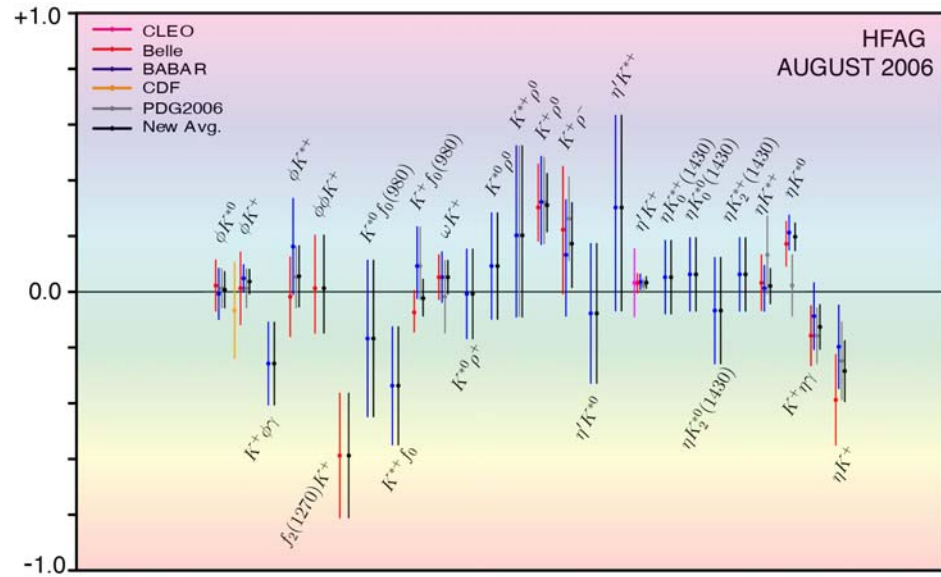
$$\mathcal{A}_{CP} = -0.01 \pm 0.13 \pm 0.02$$

Searches for direct CP violation

CP Asymmetry in Charmless B Decays



CP Asymmetry in Charmless B Decays



- There is a huge effort from the B-factories in trying to observe direct CP violation.
- Two signals observed so far in $B^0 \rightarrow \pi^+ \pi^-$ and $K^+ \pi^-$
(Y.J. Kwon's talk this morning)

Summary

- Rare B decays provide a useful testing ground for theoretical calculations.
 - Loop dominated can also be used to constrain possible physics contributions beyond the standard model.
 - Provide constraints of the unitarity triangle that compliment the angle and mixing measurements.
 - $B^+ \rightarrow K^{*0} \rho^+$ can be used to constrain theoretical uncertainty in the determination of α .
- The B-factories have recorded $1ab^{-1}$ of data and will double this by the end of 2008.
 - More stringent bounds on the triangle and NP model parameter space to come.